

## Arithmetic Progressions

- Look at the list of numbers 1, 3, 5, 7,.....
- Each of the numbers in the list is called a term.
- An arithmetic progression is a list of numbers in which each term is obtained by adding a fixed number to the preceding term except the first term.
- This fixed number is called the common difference of the AP. It can be positive, negative or zero
- The general form of an AP is:  $a, a + d, a + 2d, a + 3d, \dots$
- An AP with finite number of terms is a finite AP. That means the AP has a last term.
- An AP which does not have finite number of terms is an infinite AP. That means the AP does not have a last term.  $n^{\text{th}}$  term of an AP:

Let  $a_1, a_2, a_3, \dots$  Be an AP whose first term  $a_1$  is  $a$  and the common difference is  $d$ .

Then,

The **Second** term  $a_2 = a + d = a + (2 - 1) d$

The **third** term  $a_3 = a_2 + d = (a + d) + d = a + 2d = a + (3 - 1) d$

The **fourth** term  $a_4 = a_3 + d = (a + 2d) + d = a + 3d = a + (4 - 1) d$

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Looking at the pattern, we can say that the  $n^{\text{th}}$  term  $a_n = a + (n - 1) d$ .

So, the  $n^{\text{th}}$  term  $a_n$  of the AP with first term  $a$  and common difference  $d$  is given by  $a_n = a + (n - 1) d$ .

Sum on  $n$  terms in an AP:

The sum of the first  $n$  terms of an AP is given by  $S = - (n - 1) d$